### 1 SYSTEM AND METHOD OF MOLECULE COUNTING USING FLUCTUATION

### 2 ENHANCED SENSORS

# 3 Cross-reference to Related Applications

- 4 [0001] This application is a continuation-in-part of
- 5 commonly-assigned, pending, Non-Provisional Application No.
- 6 10/677,684, entitled System and Method of Fluctuation Enhanced
- 7 Gas-Sensing using SAW devices, filed October 02, 2003, herein
- 8 incorporated by reference. Application No. 10/677,684 claims the
- 9 benefit of Provisional Application No. 60/475,058, filed May 30,
- 10 2003, also, herein incorporated by reference.

## 11 Federally-Sponsored Research and Development

- 12 [0002] The SYSTEM AND METHOD OF MOLECULE COUNTING USING
- 13 FLUCTUATION ENHANCED SENSORS is available for licensing for
- 14 commercial purposes. Licensing and technical inquiries may be
- 15 directed to the Office of Patent Counsel, Space and Naval
- 16 Warfare Systems Center, San Diego, Code 20012, San Diego, CA,
- 17 92152; telephone (619)553-3001, facsimile (619)553-3821.

## 1 Summary of the Invention

In one aspect of the invention, a method for analyzing 2 a chemical analyte includes the steps of: (1) generating a 3 fluctuation output signal in response to a plurality of 4 frequency fluctuations in the oscillatory output signal of a 5 surface acoustic wave (SAW) sensor where the fluctuations are 6 7 responsive to adsorption of molecules on a surface of the SAW 8 sensor; (2) transforming the fluctuation output signal into an 9 amplitude density signal that represents the amplitude density 10 of the frequency fluctuations; and (3) generating an analyte output signal that is representative of a total number of the 11 12 adsorbed molecules. In another aspect of the invention, a chemical sensor 13 [0004] system is provided that includes a chemical sensor arranged to 14 15 produce an oscillatory output signal responsive to adsorption of 16 molecules of a chemical analyte by a primary surface of the 17 sensor. The chemical sensor system also includes: measurement means for measuring a plurality of frequency fluctuations of the 18 oscillatory output signal of the sensor; amplitude density means 19 20 for generating an amplitude density signal representative of the amplitude density of the frequency fluctuations; and decision 21 22 means for generating an analyte output signal representative of

- 1 a total number of the adsorbed molecules in response to the
- 2 amplitude density signal.
- 3 [0005] In still another aspect of the invention a computer
- 4 program product (CPP) is provided that includes a machine-
- 5 readable recording medium and a first, second, and third
- 6 instruction means recorded on the medium for use with a chemical
- 7 sensor system that includes a chemical sensor arranged to
- 8 produce an oscillatory output signal when exposed to a chemical
- 9 analyte. The first, second, and third instruction means are
- 10 recorded on the medium for directing the chemical sensor system
- 11 to: (1) generate a fluctuation output signal in response to a
- 12 plurality of frequency fluctuations in the oscillatory output
- 13 signal of the chemical sensor; (2) generate an amplitude density
- 14 signal representative of the amplitude density of the frequency
- 15 fluctuations; and (3) generate an analyte output signal that
- 16 identifies a total number of adsorbed molecules of the analyte.
- 17 [0006] In yet another aspect of the invention, a method for
- 18 analyzing a chemical analyte includes the steps of: (1)
- 19 generating a surface acoustic wave across a surface of a
- 20 structure; (2) transducing the surface acoustic wave into an
- 21 oscillatory output signal; (3) generating a fluctuation output
- 22 signal in response to a plurality of frequency fluctuations in
- 23 the oscillatory output signal, where the fluctuations are

- 1 responsive to the adsorption of molecules of the chemical
- 2 analyte on the surface of the structure; (4) generating an
- 3 amplitude density histogram in response to the fluctuation
- 4 output signal; and (5) generating an analyte output signal that
- 5 identifies a total number n of the adsorbed molecules.

## 1 Brief description of the Drawings

- 2 [0007] FIG. 1 is a block diagram of a chemical sensor system
- 3 in accordance with the system and method of molecule counting
- 4 using fluctuation enhanced sensors.
- 5 [0008] FIG. 2 is a block diagram of a surface of a chemical
- 6 sensor in accordance with the system and method of molecule
- 7 counting using fluctuation enhanced sensors.
- 8 [0009] FIG. 3 is a flow-chart of a method in accordance with
- 9 the system and method of molecule counting using fluctuation
- 10 enhanced sensors.
- 11 [0010] FIG. 4 is a computer program product in accordance
- 12 with the system and method of molecule counting using
- 13 fluctuation enhanced sensors.
- 14 [0011] FIG. 5 is a view showing theoretical amplitude density
- 15 histograms in accordance with the system and method of molecule
- 16 counting using fluctuation enhanced sensors.
- 17 [0012] FIG. 6 is a view showing simulated measurements of
- 18 amplitude density functions in accordance with the system and
- 19 method of molecule counting using fluctuation enhanced sensors.

# 1 Description of Some Embodiments

- 2 [0013] Following is a glossary of terms used to describe the
- 3 system and method for molecule counting using fluctuation
- 4 enhanced sensors. The definitions set forth in the glossary are
- 5 representative of the intended meanings as used herein.
- 6 GLOSSARY
- 7 [0014] The term "amplitude density" g(U) may be
- 8 mathematically defined as follows:  $P(U_0,dU) = g(U) \cdot dU$ , where
- 9  $P(U_{\circ},dU)$  is the probability of finding the amplitude around the
- 10 amplitude value  $U_0$  in the range of dU width. The amplitude
- 11 density may be approximated by an amplitude density histogram of
- 12 the measured time series.
- 13 [0015] The term "bandpass filter" means a wave filter that
- 14 attenuates frequencies on one or both sides of a single
- 15 transmission band.
- 16 [0016] The term "chemical analyte" means a substance being
- 17 measured in an analytical procedure.
- 18 [0017] The term "chemical sensor" means a device that
- 19 responds to chemical stimulus.
- 20 [0018] The term "diffusion coefficient" means a coefficient
- 21 used to represent the random motion of the molecules on the
- 22 surface of the SAW device. By way of example, the diffusion

- 1 coefficient may be represented by:  $\left\langle r^{2}\right\rangle \! \propto D \cdot t \,,$  where r is the
- 2 distance traveled by an analyte molecule, D is the diffusion
- 3 coefficient, t is elapsed time, and where the angle brackets
- 4 represent the arithmetic mean operation.
- 5 [0019] The term "frequency counter" means an instrument in
- 6 which frequency is measured by counting the number of cycles
- 7 occurring during an established time interval.
- 8 [0020] The term "machine-readable recording medium" means a
- 9 physical material in or on which data may be represented wherein
- 10 the data can be read by an input unit for storage, processing,
- 11 or display.
- 12 [0021] FIG. 1 shows a block diagram of a gas-sensing SAW
- 13 device 102 in a chemical sensor system 100, in accordance with
- 14 the system and method of molecule counting using fluctuation
- 15 enhanced sensors. SAW device 102 typically includes two
- 16 electrode pairs 106 and 108. Although SAW device 102 is shown in
- 17 FIG. 1 as only having two electrodes, it is recognized that any
- 18 number of electrode pairs for the generation and measurement of
- 19 surface propagating waves on a SAW device may be implemented.
- 20 The space between electrode pairs 106 and 108 is referred to as
- 21 the gas-sensing region 110 or the "sweetspot". In operation, the
- 22 extra inertial mass of adsorbed molecules 112 decreases the
- 23 propagation velocity of a generated surface acoustic wave 101

- 1 and thus the delay time increases between electrode pairs 106
- 2 and 108. The propagation velocity of surface acoustic wave 101
- 3 is inversely proportional to the number of adsorbed molecules
- 4 112 in the gas-sensing region 110.
- 5 [0022] The gas molecules 112 adsorbed on the surface of SAW
- 6 device 102 execute a surface diffusion process, which is
- 7 essentially a random walk over the entire surface of SAW device
- 8 102. Assuming that SAW device 102 has a thin and substantially
- 9 uniform coating over the whole surface, the diffusion
- 10 coefficient D of the adsorbed gas molecules is constant along
- 11 the entire surface of SAW device 102. Alternatively, the surface
- 12 of SAW device 102 may include one or more active zones. FIG. 2
- 13 shows an alternative surface 200 of SAW device 102. Asymmetric
- 14 surface 200 includes active zone 202 and passive zone 204. Also
- 15 included on asymmetric surface 200 is diffusion barrier 206 that
- 16 restricts diffusion to zones 202 and 204.
- 17 [0023] Due to independent random walking of each molecule
- 18 across the surface of SAW device 102, the instantaneous number
- N(t) of molecules over gas-sensing region 110 will fluctuate with
- 20 respect to time. Therefore, chemical sensor system 100 will have
- 21 fluctuations of the mean oscillation frequency  $f_{\rm osc}$  and the
- 22 instantaneous value  $\Delta f_{osc}(t)$  of the frequency deviation from the
- 23 frequency of the gas-molecule-free case will be proportional to

- 1 N(t). The dynamical properties of the fluctuations in N(t) and
- 2 the induced frequency fluctuations  $\Delta f_{osc}(t)$  will be determined by
- 3 the value of D, the geometry of SAW device 102, the gas-sensing
- 4 region 110, and the active and passive zones.
- 5 [0024] SAW device 102, in FIG. 1, is not drawn to scale and
- 6 is shown as having a total length 104a, total width 104b, and
- 7 gas-sensing region length 104c. The primary surface of SAW
- 8 device 102 has an area defined by total length 104a and total
- 9 width 104b. By way of example, SAW device 102 may detect one
- 10 type of molecule with a characteristic diffusion time constant  $au_{
  m L}$
- 11 that is much shorter than a characteristic adsorption-desorption
- 12 time constant  $au_{\mathrm{ad}}$  . The characteristic diffusion time  $au_{\mathrm{L}}$  may be
- 13 defined as  $\tau_L = \frac{L^2}{D}$  , where L is the total length 104a of SAW
- 14 device 102 and D is the diffusion coefficient of the adsorbed
- 15 gas molecules 112. The characteristic adsorption-desorption time
- 16 constant  $au_{ad}$  may be defined as  $au_{ad} = \frac{ au_a \cdot au_d}{ au_a + au_d}$ , where  $au_a$  is the
- 17 adsorption time constant and  $au_{
  m d}$  is the desorption time constant.
- 18 [0025] The probability of a molecule residing in a zone on
- 19 the surface of SAW device 102 is substantially proportional to
- 20 the area of the zone in question. The probability density of the
- 21 molecule distribution is approximately:

$$P(r,n) = \frac{n!}{r!(n-r)!} \cdot p^{r} \cdot (1-p)^{n-r},$$
 EQ. 1

- 1 where n and r are nonnegative integers,  $r \le n$ , n represents the
- 2 total number of molecules on the surface of SAW device 102, r
- 3 represents the number of molecules on an active zone, and p is
- 4 represented by:  $p = \frac{\mu_{\rm active}}{\mu_{\rm total}}$ , where  $\mu_{\rm total}$  is the total area of the
- 5 surface of the SAW device 102 and  $\mu_{ ext{active}}$  is the area of the active
- 6 zone.
- 7 [0026] Chemical sensor system 100 optionally includes a
- 8 bandpass filter 114, for selecting an oscillatory mode of
- 9 operation, and amplifier 116 coupled to electrodes 106 and 108.
- 10 [0027] Also included in chemical sensor system 100 is
- 11 measurement means for measuring a plurality of frequency
- 12 fluctuations in oscillatory output signal 117. FIG. 1 shows an
- 13 example of measurement means as frequency fluctuation counter
- 14 118. There are various ways that frequency fluctuation counter
- 15 118 may measure these frequency fluctuations. One such method is
- 16 heterodyning, that is, nonlinearly mixing the oscillatory output
- 17 signal with a noiseless oscillator signal with a frequency close
- 18 to the fluctuating signal frequency. At the output of this
- 19 mixing, the difference of the two frequencies is identified and
- 20 the relative fluctuations will increase. Zero crossings may then
- 21 be counted using short-term measurements. The zero crossing

- 1 measurements would give the actual frequency, while the mean of
- 2 these would result in the mean frequency. The frequency
- 3 fluctuations, using this heterodyning method, are the difference
- 4 of the actual and the mean frequencies.
- 5 [0028] In the case of an asymmetric surface design, as shown
- 6 in FIG. 2, the instantaneous amplitude, which is output by
- 7 frequency counter 118, is:  $U_{as}(t) = K \cdot N_A(t)$ , where K is a
- 8 calibration constant and  $N_{\scriptscriptstyle A}(t)$  is the instantaneous number of
- 9 molecules in the active zone.
- 10 [0029] Chemical sensor system 100 also includes amplitude
- 11 density means for generating an amplitude density signal that is
- 12 representative of the amplitude density of the frequency
- 13 fluctuations measured in frequency fluctuation counter 118. FIG.
- 14 1 shows and example of amplitude density means as statistical
- 15 analyzer 120. Statistical analyzer 120 may generate the
- 16 amplitude density signal by way of generating an amplitude
- 17 density histogram of the measured time series output by
- 18 frequency fluctuation counter 118. By way of example, FIG. 6
- 19 (a), (b), or (c) may represent outputs of statistical analyzer
- 20 120.
- 21 [0030] A decision means for generating an analyte output
- 22 signal 124, that is representative of a total number n adsorbed
- 23 molecules of the analyte 112, is also included in chemical

- 1 sensor system 100. Alternatively, analyte output signal may
- 2 represent a total number of molecules of the analyte 112 in a
- 3 designated volume. FIG. 1 shows an example of decision means as
- 4 pattern recognizer 122. Pattern recognizer correlates patterns
- 5 in the measured amplitude density signal to a theoretical
- 6 amplitude density histogram generated with EQ. 1. As an example,
- 7 pattern recognizer 122 may utilize a look-up table, a neural
- 8 network, or other processing means.
- 9 [0031] FIG. 3 illustrates a method 300 in accordance with the
- 10 system and method of molecule counting using fluctuation
- 11 enhanced sensors. Method 300 utilizes statistical analysis of
- 12 the dynamics of measured frequency fluctuations of a surface
- 13 acoustic wave (SAW) device that is arranged to produce an
- 14 oscillatory output signal when exposed to a chemical analyte.
- 15 Step 302 includes generating a fluctuation output signal in
- 16 response to a plurality of frequency fluctuations  $\Delta f_{osc}$  of the
- 17 oscillatory output signal. There are various methods that may be
- 18 implemented for the measurement of the frequency fluctuations.
- 19 One such method is heterodyning, that is nonlinearly mixing the
- 20 oscillatory output signal with a noiseless oscillator signal
- 21 with a frequency close to the fluctuating signal frequency. At
- 22 the output of this mixing, the difference of the two frequencies
- 23 is identified and the relative fluctuations will increase. Zero

- 1 crossings may then be counted using short-term measurements. The
- 2 zero crossing measurements would give the actual frequency,
- 3 while the mean of these would result in the mean frequency. The
- 4 frequency fluctuations, using this heterodyning method, are the
- 5 difference of the actual and the mean frequencies.
- 6 [0032] Step 304 transforms the fluctuation output signal into
- 7 an amplitude density signal that is representative of the
- 8 amplitude density. The amplitude density may be described,
- 9 theoretically, by EQ. 1.
- 10 [0033] Using the measured amplitude density implies strongly
- 11 enhanced selectivity and sensitivity. One factor contributing to
- 12 higher sensitivity is the fact that, due to the particular shape
- 13 of the amplitude density of diffusion processes, the diffusion
- 14 noise can be easily distinguished from other sensor noise
- 15 processes, such as adsorption-desorption and thermal noise.
- 16 [0034] The strongly enhanced selectivity also stems from the
- 17 fact that the amplitude density is a pattern, not a single
- 18 number. Therefore, the strength and the shape of the amplitude
- 19 density contains information about the number of gas molecules.
- 20 [0035] Lastly, step 306 generates an analyte output signal
- 21 that is representative of a total number n adsorbed molecules of
- 22 the chemical analyte, if the amplitude density signal
- 23 corresponds to a theoretical amplitude density function. As an

- 1 example, the characteristic signal may be generated by way of a
- 2 pattern recognizer, a look-up table, or other processing means.
- 3 [0036] FIG. 4 illustrates a computer program product (CPP)
- 4 400, in accordance with the system and method of molecule
- 5 counting using fluctuation enhanced sensors. CPP 400 is for use
- 6 with a chemical sensor system that includes a chemical sensor
- 7 arranged to produce an oscillatory output signal when exposed to
- 8 a chemical analyte. CPP 400 includes a machine-readable
- 9 recording medium 402 and a first, second, and third instruction
- 10 means, recorded on the recording medium 402.
- 11 [0037] First instruction means 404 are for directing the
- 12 chemical sensor system to generate a fluctuation output signal
- 13 in response to a plurality of frequency fluctuations in the
- 14 oscillatory output signal generated by the chemical sensor.
- 15 There are various ways that first instruction means 404 may
- 16 direct the chemical sensor system to measure these frequency
- 17 fluctuations. One such method is heterodyning, that is
- 18 nonlinearly mixing the oscillatory output signal with a
- 19 noiseless oscillator signal with a frequency close to the
- 20 fluctuating signal frequency. At the output of this mixing, the
- 21 difference of the two frequencies is identified and the relative
- 22 fluctuations will increase. Zero crossings may then be counted
- 23 using short-term measurements. The zero crossing measurements

- 1 would give the actual frequency, while the mean of these would
- 2 result in the mean frequency. The frequency fluctuations, using
- 3 this heterodyning method, are the difference of the actual and
- 4 the mean frequencies.
- 5 [0038] Second instruction means 406 are for directing the
- 6 chemical sensor system to generate an amplitude density signal
- 7 that is representative of the amplitude density of the frequency
- 8 fluctuations in the oscillatory output signal. By way of
- 9 example, second instruction means 406 may direct the chemical
- 10 sensor system to generate the amplitude density signal through
- 11 generation of an amplitude density histogram of the measured
- 12 time series of frequency fluctuations in the instantaneous
- 13 frequency.
- 14 [0039] Third instruction means 408 are for directing the
- 15 chemical sensor system to generate an analyte output signal that
- 16 identifies a total number n molecules of the chemical analyte,
- 17 if the amplitude density signal corresponds to a theoretical
- 18 amplitude density function. By way of example, the total number
- 19 of n molecules may represent the total number of molecules on
- 20 the surface of the chemical sensor. Alternatively, analyte
- 21 output signal may represent the total number of molecules in a
- 22 volume. Also, as an example, third instruction means 408 may

- 1 utilize a look-up table, a neural network, or other processing
- 2 means.
- 3 [0040] Optionally included in CPP 400 is a fourth
- 4 instruction means, recorded on the recording medium 402 for
- 5 directing the chemical sensor system to correlate patterns in
- 6 the amplitude density signal to the theoretical density
- 7 function, as generated by EQ. 1.
- 8 [0041] FIG. 5 illustrates theoretical amplitude density
- 9 histograms in accordance with the system and method of molecule
- 10 counting using fluctuation enhanced sensors. The three
- 11 histograms shown were all generated utilizing EQ.1, where p=0.5,
- 12 and n=1, 2, and 5, respectively.
- 13 [0042] FIG. 6 illustrates simulated measurements of the
- 14 amplitude density functions in accordance with the system and
- 15 method of molecule counting using fluctuation enhanced sensors.
- 16 By way of example, FIG. 6 may show outputs of the statistical
- 17 analyzer 120, of FIG. 1. These measured amplitude densities
- 18 could then be compared to the theoretical amplitude density
- 19 histograms, as shown in FIG. 5, to determine the total number of
- 20 molecules on the surface of the SAW device.